

**Prime Time** is a chapter, that focuses on the basic concepts of prime and composite numbers, factors, multiples, and divisibility rules. It lays the foundation for number theory and is useful for competitive exams

### IMPORTANT CONCEPTS

- **Factor:** A number that divides another number exactly.

Example: Factors of 12  $\rightarrow$  1, 2, 3, 4, 6, 12

- **Multiple:** A number that is the product of a given number and an integer.

Example: Multiples of 3  $\rightarrow$  3, 6, 9, 12, ...

- **Prime Number:** A number greater than 1 that has only two factors: 1 and itself.

Example: 2, 3, 5, 7, 11

- **Composite Number:** A number with more than two factors.

Example: 4, 6, 8, 9, 10

- **Co-prime Numbers:** Two numbers having only 1 as their common factor.

Example: 8 and 15

- **Perfect number:** Number for which the sum of all its factors is equal to twice the number.

Example: 28- 1, 2, 4, 7, 8, 14, 28

- **Prime numbers:** Numbers that have only two factors, namely 1 and number itself.

Ex: 2, 3, 5, 7, 11, 13, ...

- **Prime numbers from 1 to 100**

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

- **Twin primes:** Pairs of primes having a difference of 2.

Ex: (3, 5), (17, 19)

- **Divisibility Rules**

- **Divisible by 2**  $\rightarrow$  Last digit is even (0, 2, 4, 6, 8)
- **Divisible by 3**  $\rightarrow$  Sum of digits divisible by 3
- **Divisible by 4**  $\rightarrow$  Last two digits divisible by 4
- **Divisible by 5**  $\rightarrow$  Last digit is 0 or 5

- **Divisible by 7** → Double the last digit and subtract it from the remaining part of the number
  - **Divisible by 6** → Divisible by both 2 and 3
  - **Divisible by 9** → Sum of digits divisible by 9
  - **Divisible by 10** → Last digit is 0
  - **Divisible by 11** → Difference of sum of all digits at odd places and digits at even places
- **Properties of Factors and Multiples:-**
    - Every number is a factor of itself.
    - 1 is a factor of every number.
    - Factors are finite.
    - Multiples are infinite.
    - Every number is a multiple of itself.
    - Every multiple of a number is greater than or equal to the number.
  - **Prime Factorization: It means expressing a number as the product of its prime factors.**  
**Ex:**  $36 = 2 \times 2 \times 3 \times 3$
  - **Highest Common Factor (HCF):** The highest number that divides exactly two or more numbers.  
**Ex:** HCF of 12 and 18 = 6
  - **Prime Factorization: Lowest Common Multiple (LCM):** The smallest number that is a multiple of two or more numbers.  
**Ex:** LCM of 4 and 5 = 20